



ttH at ILC

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based on the paper Phys.Rev.D.84 (2011) 014033,
done by R.Yonamine, K.Ikematsu, T.Tanabe, K.Fujii, Y.Kiyo, Y.Sumino, HY,
and further advanced studies by T.Tanabe, R.Yonamine, K.Fujii, T.Price,
N. Watson, H. Tabassam, V. Martin, P.Roloff, J. Strube.



Outline :

1. Introduction
2. $t\bar{t}H$ production at the ILC
3. Simulation study at $\sqrt{s} = 500$ GeV
4. Simulation study at $\sqrt{s} = 1$ TeV
5. Summary

Introduction

- Top-quark and Higgs-boson are the two main features at the ILC

These are already known to exist.

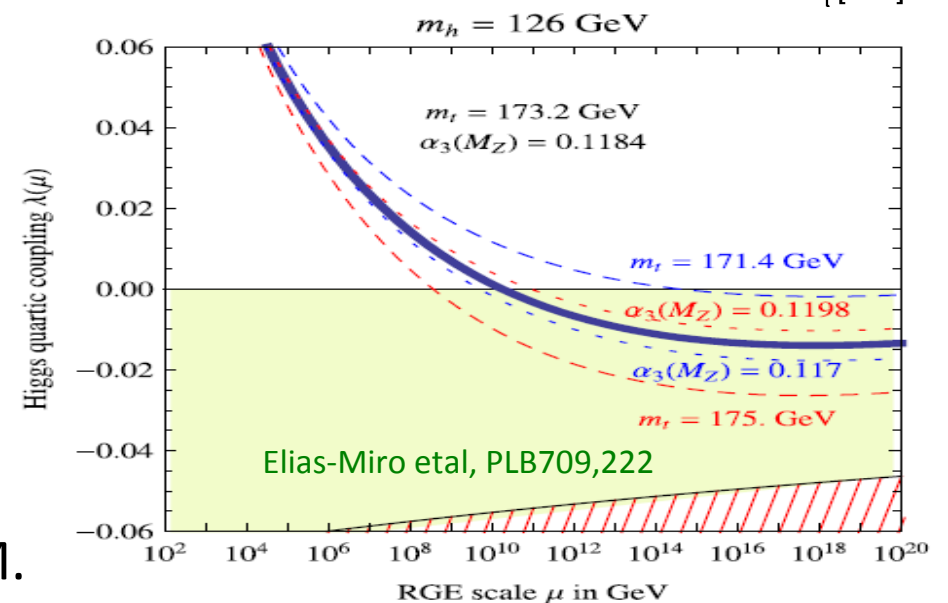
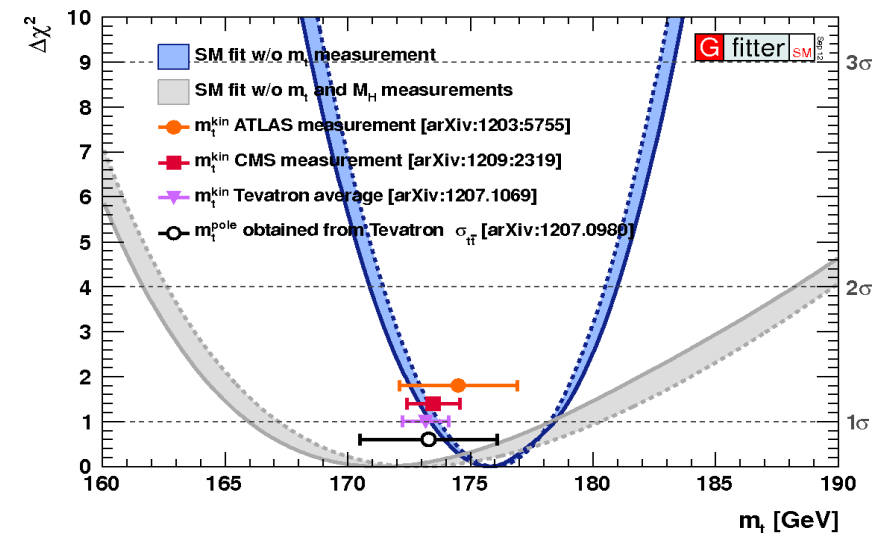
For these topics, it is very important to study and prepare what can be probed at the ILC.

- Top-quark physics: m_t , y_t , Γ_t , α_s

Especially, precision measurement of the mass is important for

- electroweak precision tests
- stability of the EW vacuum
- possible window to new physics ($y_t \sim 1$)

to disentangle the evidence of physics BSM.



Introduction

- Mass determination:

$$(\text{TeV } 8.7 \text{ fb}^{-1}) \quad m_t = 173.20 \pm 0.51(\text{stat}) \pm 0.71(\text{syst}) \text{ GeV}$$

$$(\text{LHC } 4.9 \text{ fb}^{-1}) \quad m_t = 173.3 \pm 0.5(\text{stat}) \pm 1.3(\text{syst}) \text{ GeV}$$

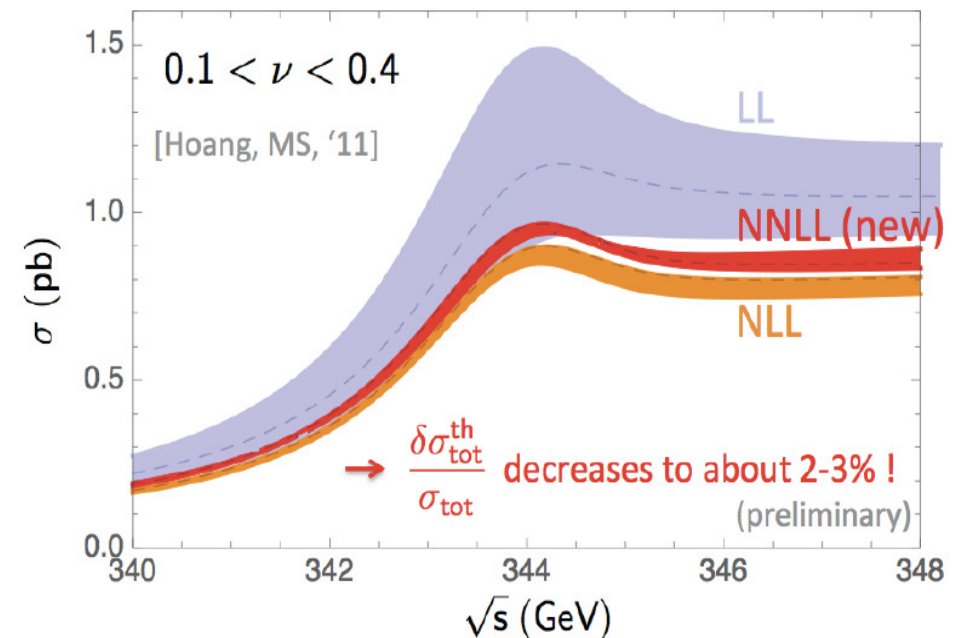
large syst. error due to mainly the Jet energy scale,
definition of the mass unclear.

At the ILC, by performing threshold scan,

$$\delta m_t \simeq 30 - 50 \text{ MeV}$$

(short distance mass),
easily converted to the $\overline{\text{MS}}$ mass

$$\delta m_t(\overline{\text{MS}}) \simeq 100 \text{ MeV}$$



Introduction

- Top-Yukawa measurements:

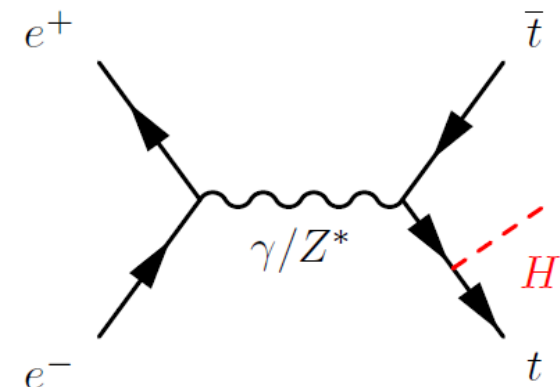
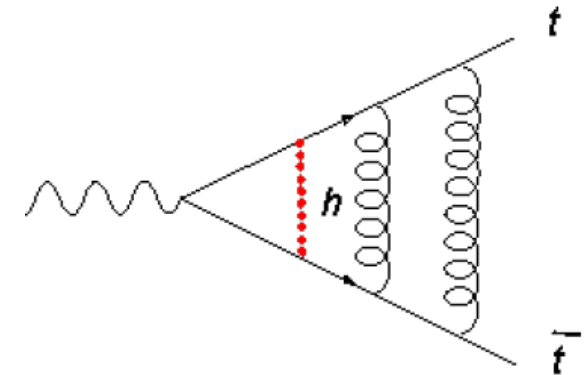
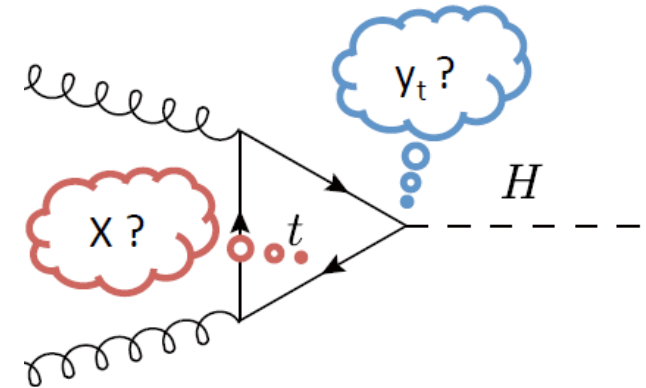
$$y_t = \frac{\sqrt{2}m_t}{v} = 0.995\dots$$

- Indirect: ggH (LHC)

ttbar at threshold
(ILC, /s=350GeV)

- Direct: ttH (LHC, ILC /s>500GeV)

Indirect determination is not conclusive
nor accurate, but able to check the consistency.



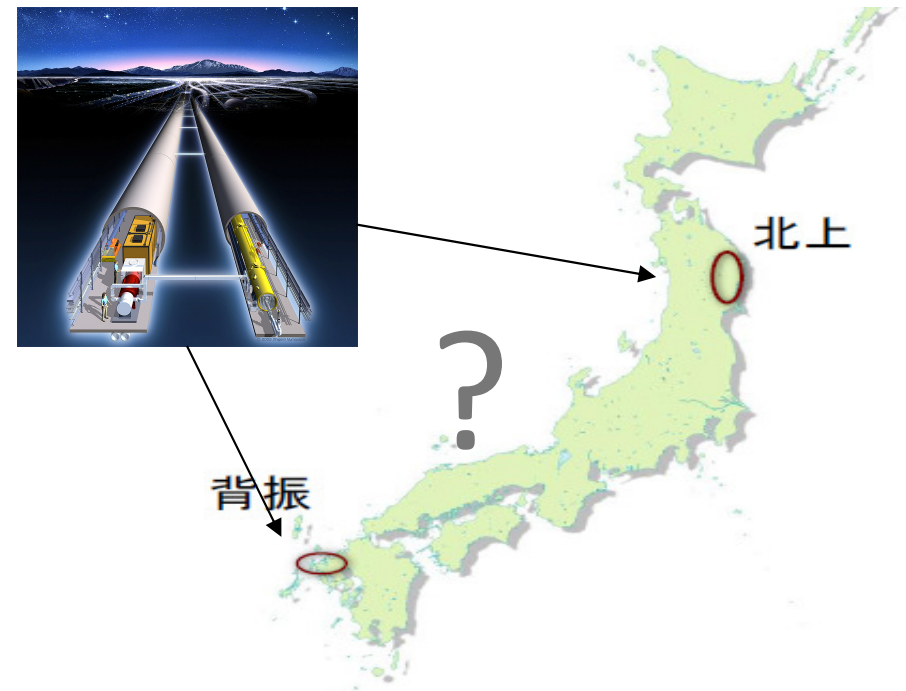
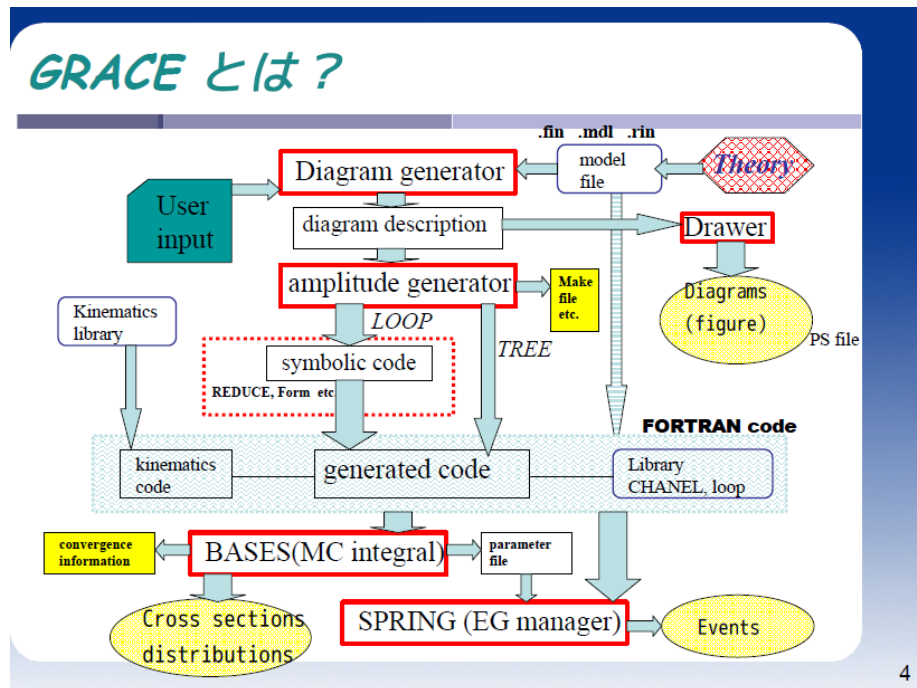
Introduction

Japanese contributions to the Top-quark and ILC Physics

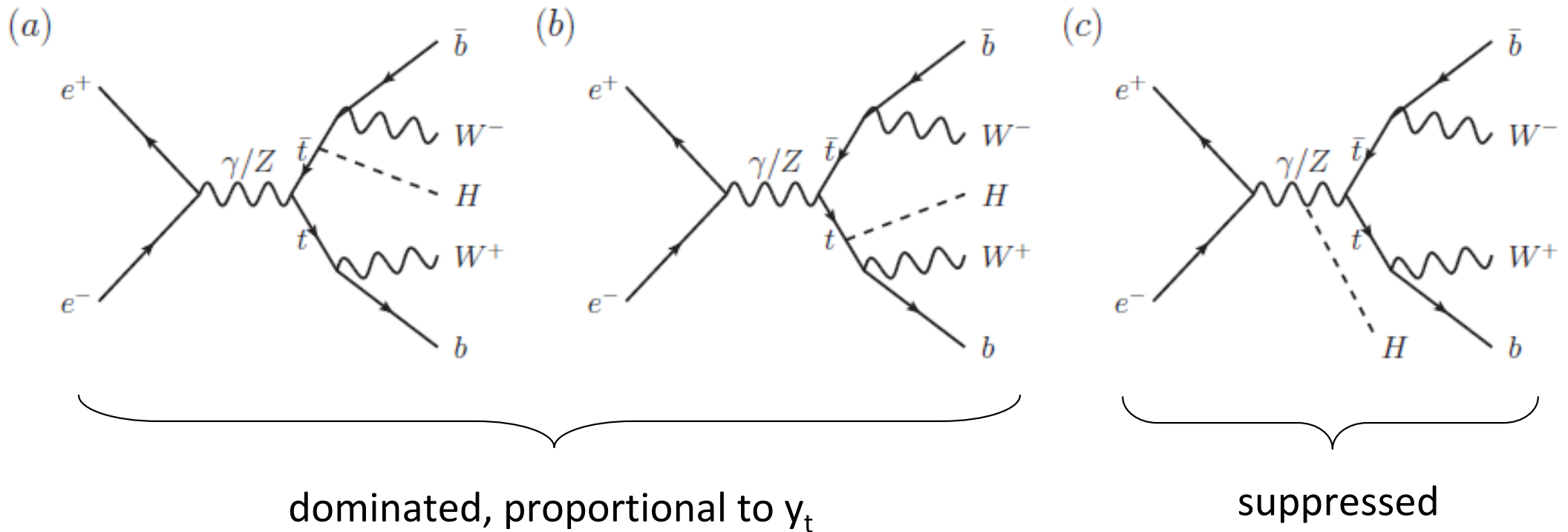
- **ILC Physics Subgroup**
- **GRACE Project (Minami-Tateya)**
- Top-QCD theorists: **Y.Sumino, Y.Kiyo,,,**

<http://www-jlc.kek.jp/subg/physics/ilcphys/>

<http://www-sc.kek.jp/>



tth process at the ILC



$$\sigma_{t\bar{t}h} \propto y_t^2$$

$$\frac{\Delta y_t}{y_t} = \frac{1}{2} \frac{\Delta \sigma}{\sigma}$$

tth process at the ILC

- Signatures, using $h \rightarrow b\bar{b}$

$$e^+e^- \rightarrow t\bar{t}h \rightarrow bjj\bar{b}jjb\bar{b} \quad (8j)$$

$$\rightarrow b\ell\nu\bar{b}jjb\bar{b} \quad (6j+1)$$

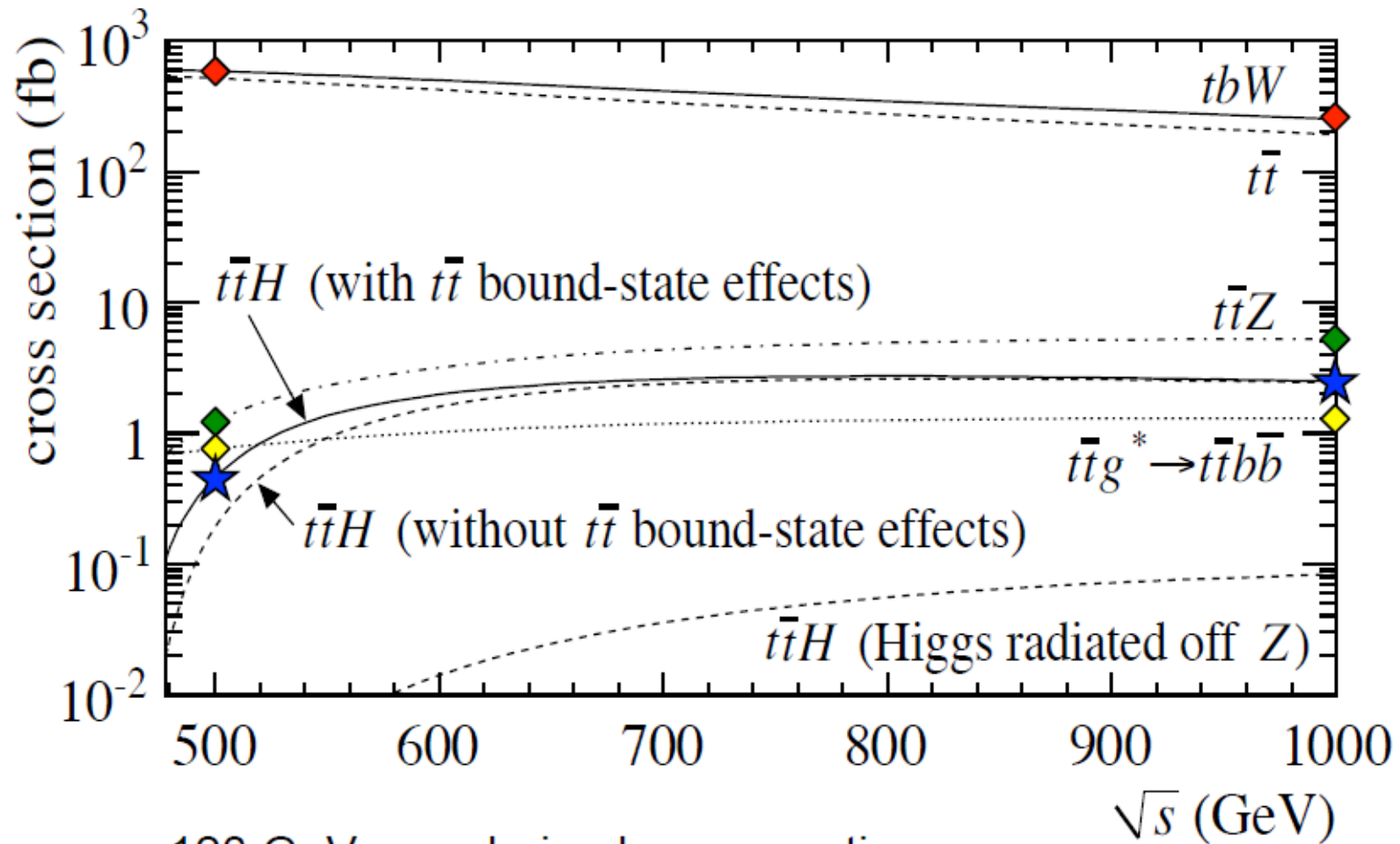
- SM Backgrounds:

$$t\bar{t}Z, \quad t\bar{t}g^* \quad \text{where } Z, g^* \rightarrow b\bar{b} \quad (\text{irreducible})$$

$$t\bar{t} \quad (tbW) \quad (\text{large cross-section})$$

tth process at the ILC

ttH , ttZ , ttg^* , tt



$m_H = 120$ GeV, unpolarized cross sections

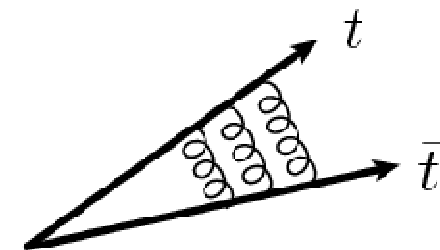
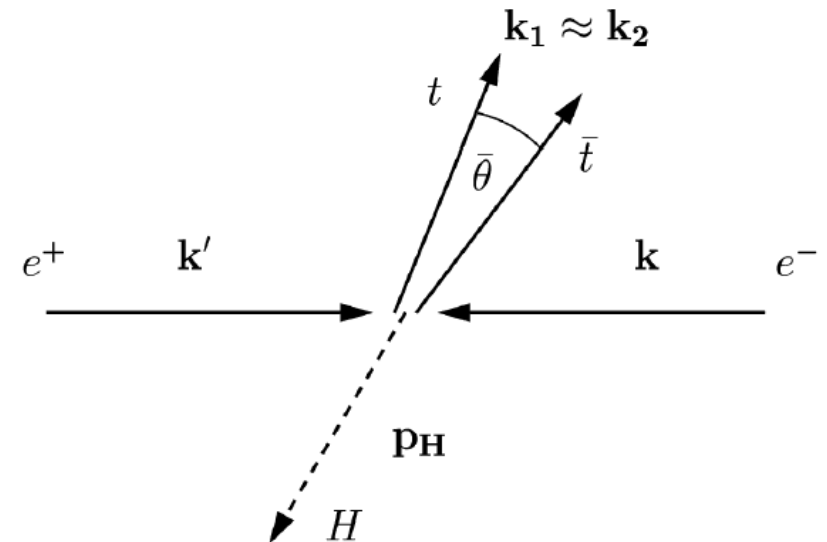
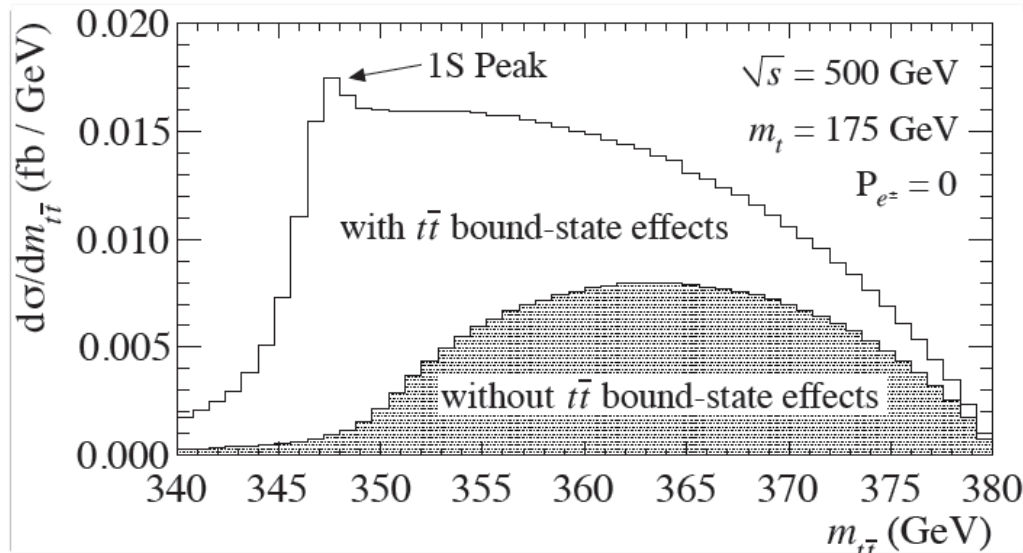
Threshold correction

Farrel, Hoang(05,06)

- At $\sqrt{s}=500$ GeV, threshold correction is large

$$E_h = \frac{1}{2\sqrt{s}} \left(s + m_h^2 - m_{t\bar{t}}^2 \right)$$

The cross-section is enhanced by a factor of ~ 2 , from the $t\bar{t}$ final-state interactions (bound-state effect).

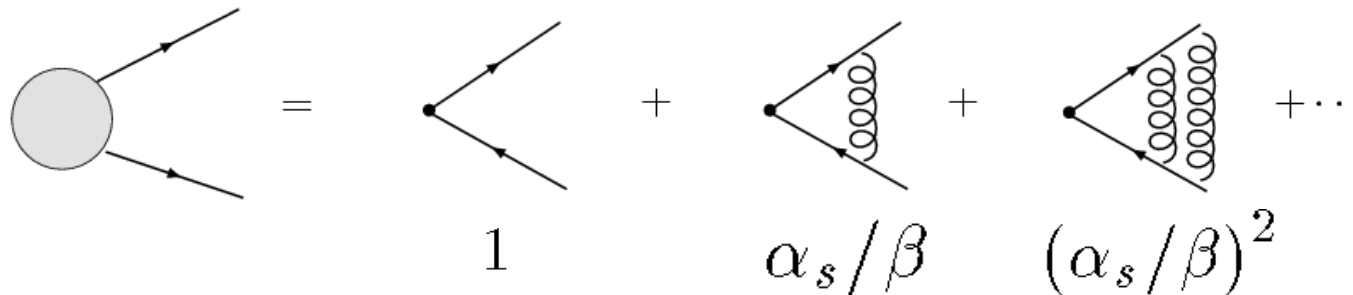


- $t\bar{t}Z$ background is also enhanced by a factor ~ 2 .

Threshold correction

Fadin,Khoze(87),,,

$$\sigma \propto \text{Im}[G(\vec{0}, E_{t\bar{t}})]$$



- Coordinate-space Green's function at the origin
- Sum-over the ladder diagrams nonperturbatively in nonrelativistic region
- NRQCD formalism to refine $O(\alpha_s \ln \beta)$ corrections

For differential cross-sections

Sumino etal(93), Fujii etal(94), Sumino,HY (10),,,

$$\frac{d\sigma}{dp_t^3} \propto \tilde{G}(\vec{p}, E_{t\bar{t}})$$

- LO in $(\alpha_s/\beta)^n$
- Smooth connection to perturbative region
- Possible to put on **event generators**



Top-Yukawa measurement

- Simulation analysis : ($\sqrt{s}=500\text{GeV}$ with 1ab^{-1} and polarization (0.8, 0.3))
 - Fast detector sim. / cut-based analysis [Yonamine etal. PRD84,014033](#)
 - Full deector sim. / multivariate analysis [T.Tanabe etal](#)
- Cuts
 - Number of leptons (Isolation)
 - Event shape (Thrust)
 - Jet clustering (Durham exclusive jet algorithm)
 - B-tagging (4 b-tagged jets)
 - Top and Higgs mass reconstruction

- Jet clustering (Durham exclusive jet algorithm):

$$Y_{ij} = \frac{\max(E_i^2, E_j^2)(1 - \cos \theta_{ij})}{E_{\text{CM}}^2}$$

ij which gives the smallest Y are merged into one.
Continue until the number of jets is 6 or 8.

$$Y_{5 \rightarrow 4(8 \rightarrow 7)} > Y_{\text{cut}} \quad \text{is useful to discriminate signal from tt BG.}$$

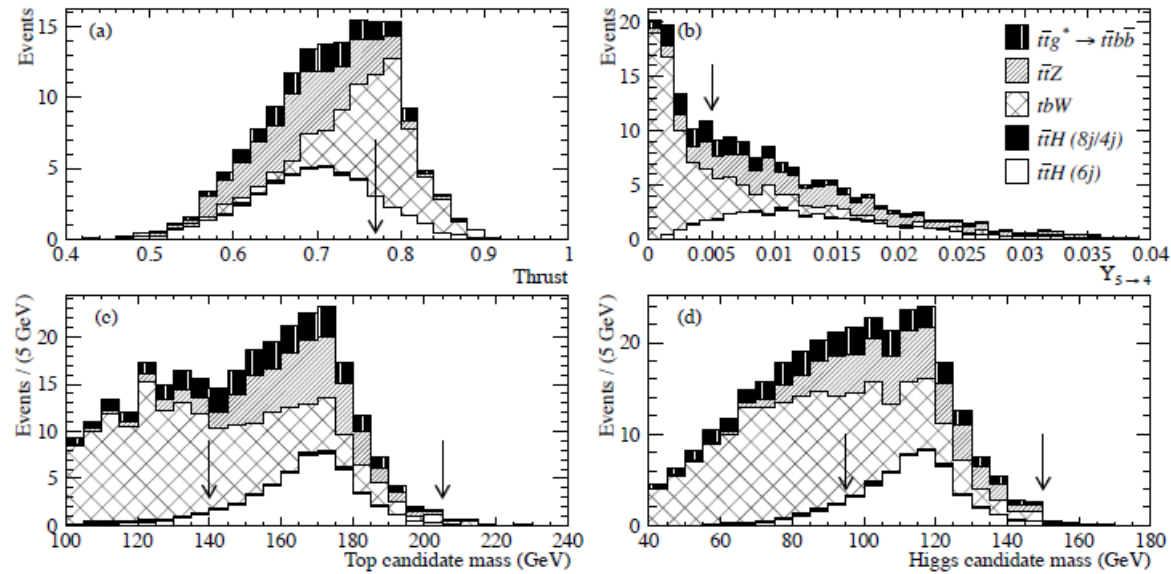
- Jet combination is fixed by minimizing chi-square;

$$\chi^2 = \frac{(m_{2j} - M_H)^2}{\sigma_H^2} + \frac{(m_{2j} - M_{W_1})^2}{\sigma_{W_1}^2} + \frac{(m_{3j} - M_{t_1})^2}{\sigma_{t_1}^2} + \left\{ \frac{(m_{2j} - M_{W_2})^2}{\sigma_{W_2}^2} + \frac{(m_{3j} - M_{t_2})^2}{\sigma_{t_2}^2} \right\}_{8j}$$

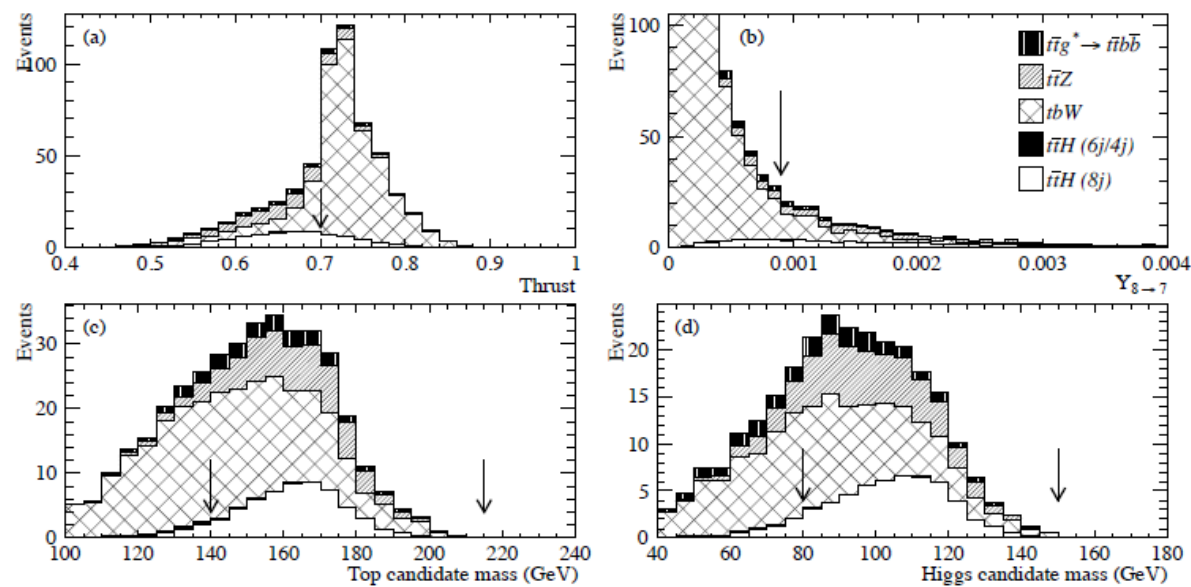
cut values

cut	6-jet + lepton	8-jet
number of isolated lepton	1	0
thrust	< 0.77	< 0.7
jet clustering	$Y_{5 \rightarrow 4} > 0.005$	$Y_{8 \rightarrow 7} > 0.00080$
b-tagging	4x b-jets	4x b-jets
top mass (GeV)	$140 < m_t < 205$	$140 < m_H < 215$
higgs mass (GeV)	$95 < m_t < 150$	$80 < m_H < 150$

- $6j + l$



- $8j$



- 6j + l

	$t\bar{t}H$ (6j)	$t\bar{t}H$ (8j)	$t\bar{t}H$ (4j)	tbW	$t\bar{t}Z$	$t\bar{t}g^* (b\bar{b})$
No cuts	282.3	289.5	68.3	980 738.5	2406.9	1159.6
Single isolated lepton	179.6	20.7	28.3	340 069.0	790.6	397.7
Thrust <0.77	145.7	18.5	19.2	144 999.0	616.7	266.0
$Y_{5\rightarrow 4} > 0.005$	125.5	16.6	9.2	12 297.7	416.2	113.7
b tagging	49.0	1.3	2.9	172.9	53.3	37.8
Mass cuts	39.5	1.2	0.4	23.0	33.9	13.2

- 8j

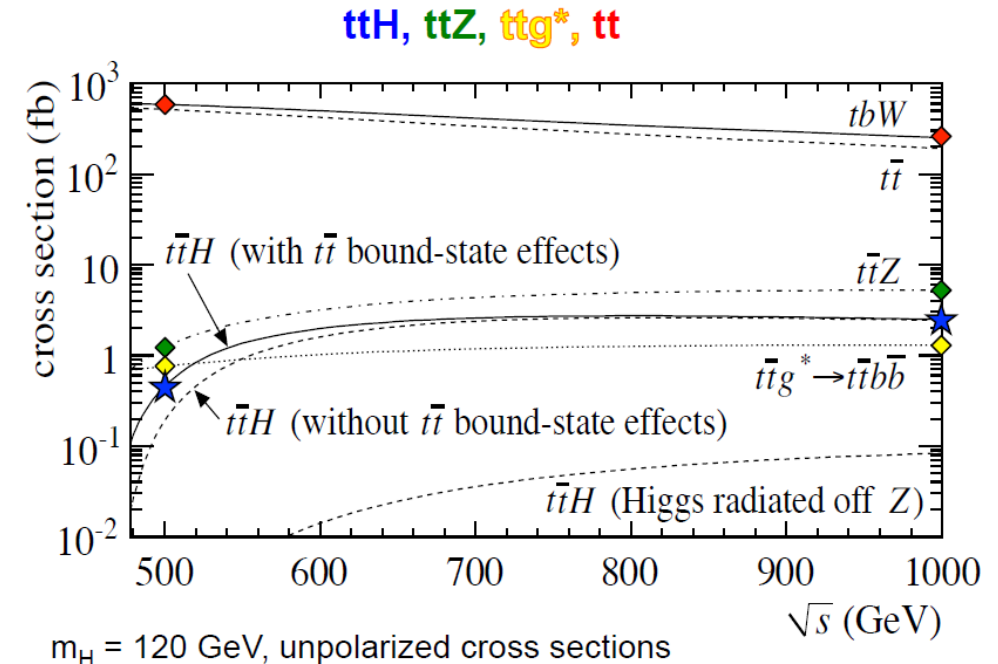
	$t\bar{t}H$ (8j)	$t\bar{t}H$ (6j)	$t\bar{t}H$ (4j)	tbW	$t\bar{t}Z$	$t\bar{t}g^* (b\bar{b})$
No cuts	289.5	282.3	68.3	980 738.5	2406.9	1159.6
Reject isolated leptons	266.3	85.6	6.6	589 716.0	1351.4	701.2
Thrust <0.7	167.7	44.0	2.7	107 227.0	818.0	311.5
$Y_{8\rightarrow 7} > 0.0009$	113.8	13.0	0.3	4048.1	349.6	67.1
b tagging	66.6	6.8	0.1	442.6	77.6	39.8
Mass cuts	50.1	0.4	0.0	75.6	47.6	14.1

3.7 σ for both modes

$$\sqrt{s} = 1 \text{ TeV}$$

- At 1TeV, signal increases (peak $\sim 800\text{GeV}$), but BG decrease
- Bound-state effects negligible
- ILD and SiD full simulation ongoing

expect to improve the accuracy



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15

	$t\bar{t}h$ (4J)	$t\bar{t}h$ (6J)	$t\bar{t}h$ (8J)	$t\bar{t}h$ ($h \not\rightarrow b\bar{b}$)	$t\bar{t}Z$	$t\bar{t}b\bar{b}$	$t\bar{t}$	Sig.
No cuts	151.39	628.73	652.77	1046.10	5332.52	1434.53	306238.26	1.16
$N_{\text{iso}} = 0$	20.87	261.17	647.92	556.71	3226.14	932.49	188911.38	1.47
$E_{\text{vis}} > 650 \text{ GeV}$	9.83	220.97	636.16	497.45	2743.54	849.34	157389.56	1.58
Thrust < 0.87	8.09	187.75	577.60	440.06	2219.68	540.88	46916.14	2.56
$Y_{78} > 0.0001$	3.65	143.55	549.52	415.51	1926.58	474.59	27472.09	3.12
$btag_4 > 0.38$	1.89	80.98	275.02	17.55	230.04	209.60	680.62	7.11
$ \cos \theta_{\text{hel}} < 0.9$	1.63	73.80	263.71	16.48	215.91	189.19	584.92	7.19
$m_t > 120 \text{ GeV}$	1.50	68.09	255.38	15.58	207.81	178.53	530.93	7.20

- Cut-based → Multivariate analysis:

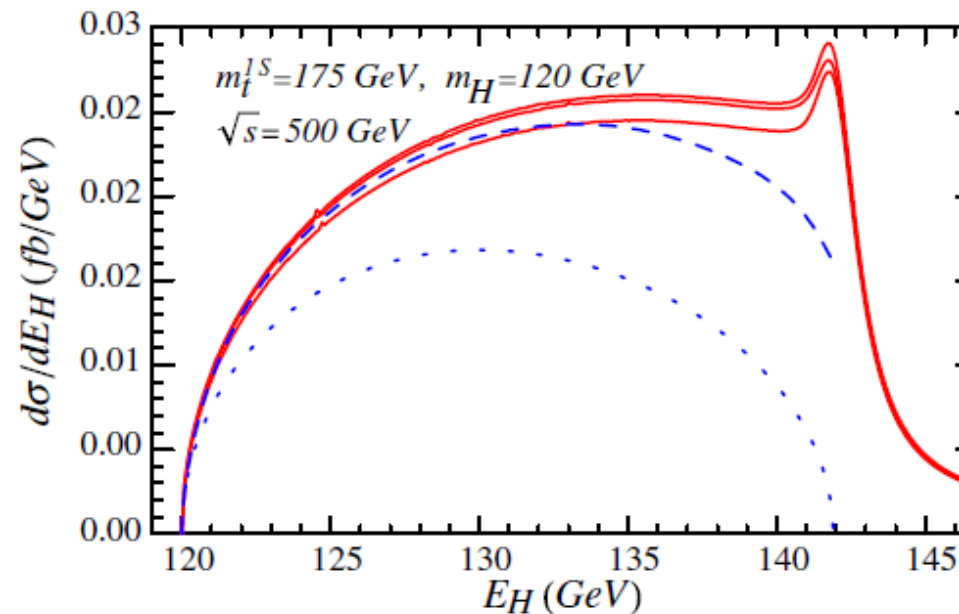
	Statistical Significance	
	Cut-based	Multivariate
$t\bar{t}h \rightarrow b\bar{q}qblvbb$	5.4	7.6
$t\bar{t}h \rightarrow b\bar{q}qbqqbb$	7.2	9.6

- Summary of the Top-Yukawa measurements:

CM Energy	500 GeV	1 TeV	
Higgs mass	125 GeV	125 GeV	
Beam polarization	(-0.8, +0.3)	(-0.8, +0.2)	
Integrated Luminosity	1 ab ⁻¹	1 ab ⁻¹	
Detector Model	ILD	ILD	SiD
$\Delta y_t/y_t$	11%	3.9%	4.0%

Theoretical uncertainty

- Theoretical prediction has several % uncertainty due to the choice of renormalization scale.
- It is a common problem for $t\bar{t}$ threshold physics (NNLL)
 - needs new idea or higher order?
- Might be improved at 1TeV where fixed-order correction is enough.



Farrel, Hoang(05,06)

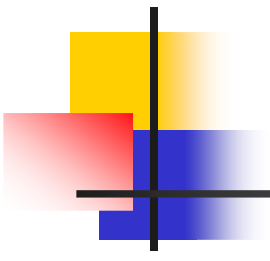


Summary

- Top-quark mass (or the Yukawa coupling) is an important input to find the evidence of the physics beyond the SM.
- Yukawa coupling of the top-quark can be directly measured at $t\bar{t}h$ production process.
- At $\sqrt{s}=500\text{GeV}$, threshold correction enhance the signal by a factor of 2.
- The expected accuracy of the measurement at the ILC is

$$\frac{\Delta y_t}{y_t} \simeq 11\% \text{ @ } \sqrt{s} = 500 \text{ GeV}, 1\text{ab}^{-1}$$
$$\frac{\Delta y_t}{y_t} \simeq 4\% \text{ @ } \sqrt{s} = 1 \text{ TeV}, 1\text{ab}^{-1}$$

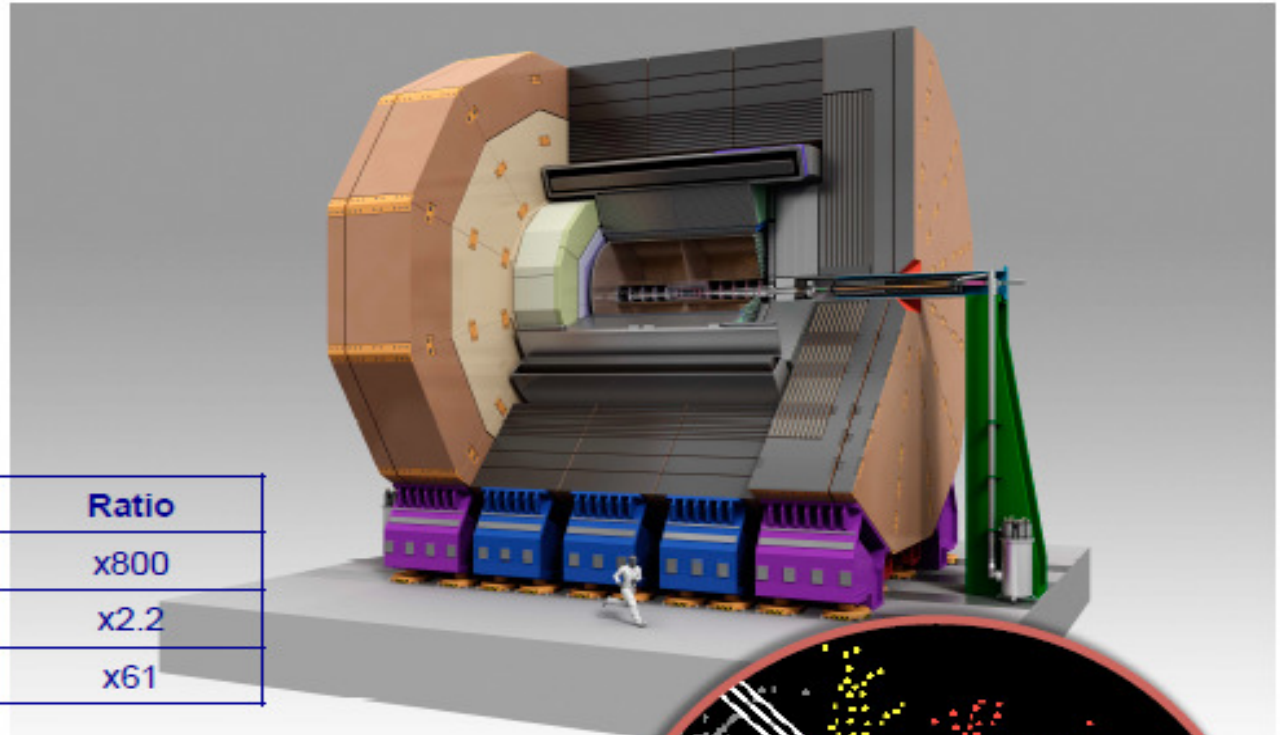
I thank T.Tanabe, R.Yonamine, K.Fujii, T.Price, N.Watson, H.Tabassam, V.Martin, P.Roloff, J.Strub, for providing their results shown in this talk.



ILD detector

- **Vertex Detector:** pixel detectors & low material budget
- **Tracker:** low material budget
- **Calorimeters:** high granularity sensors

Sensor Size	ILD	ATLAS	Ratio
Vertex	5x5 mm ²	400x50 mm ²	x800
Tracker	1x6 mm ²	13 mm ²	x2.2
ECAL	5x5 mm ² (Si)	39x39 mm ²	x61



Particle Flow Algorithm

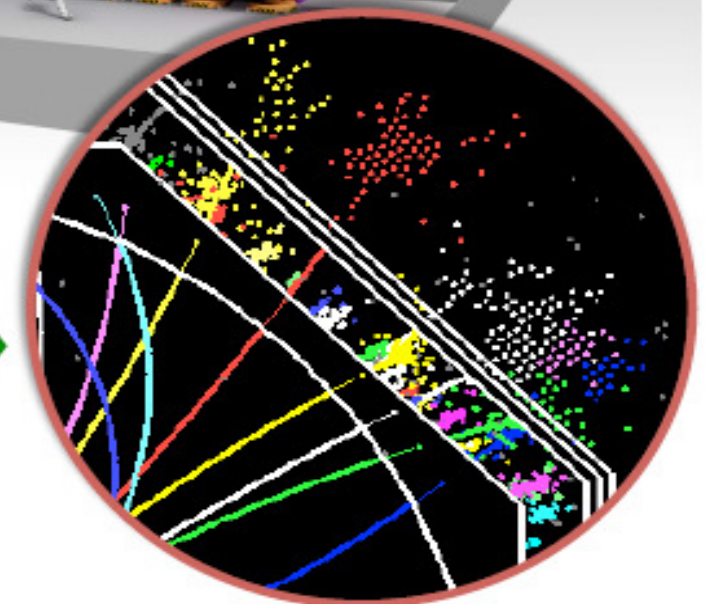
Separate calorimeter clusters at particle level

- use *best* energy measurement for *each* particle.
- offers unprecedented **jet energy resolution**

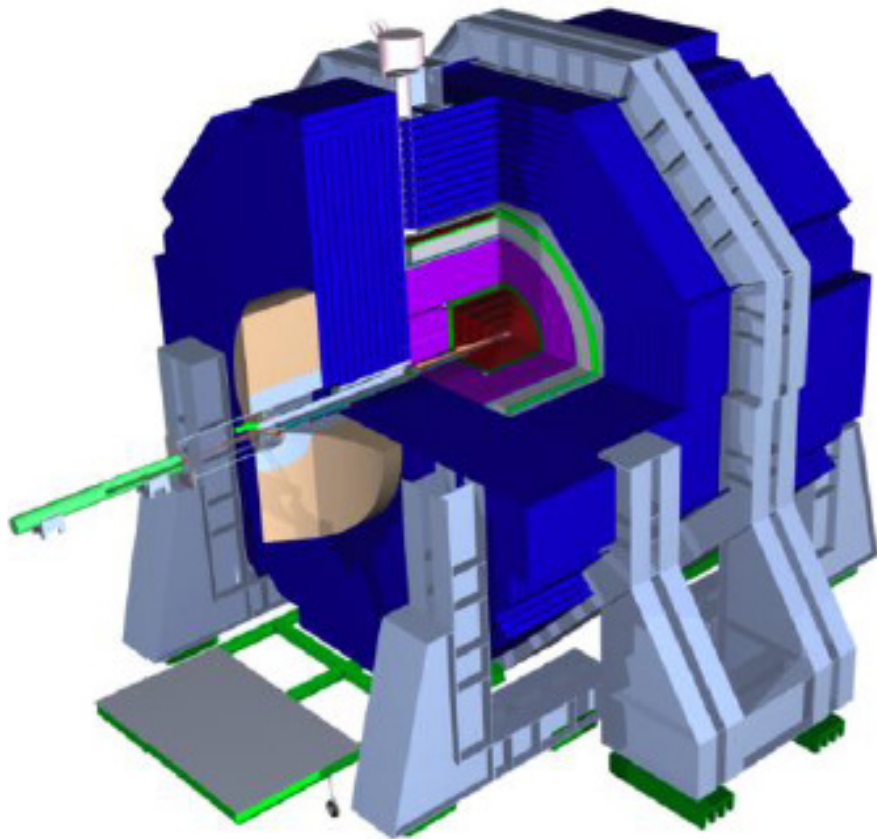
Charged Tracks → Tracker

Photons → **ECAL**

Neutral Hadrons → **HCAL**

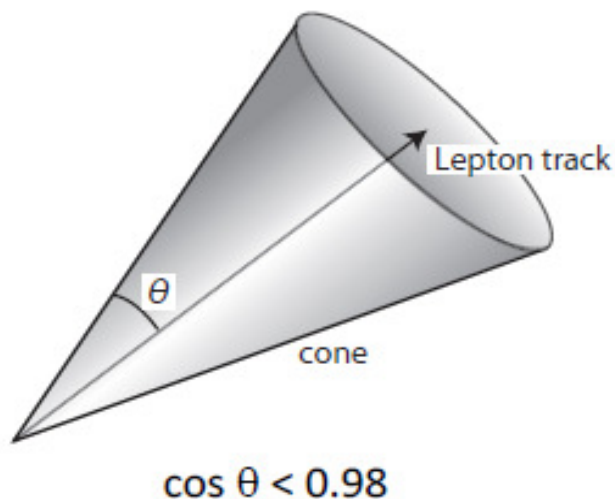


SiD detector:

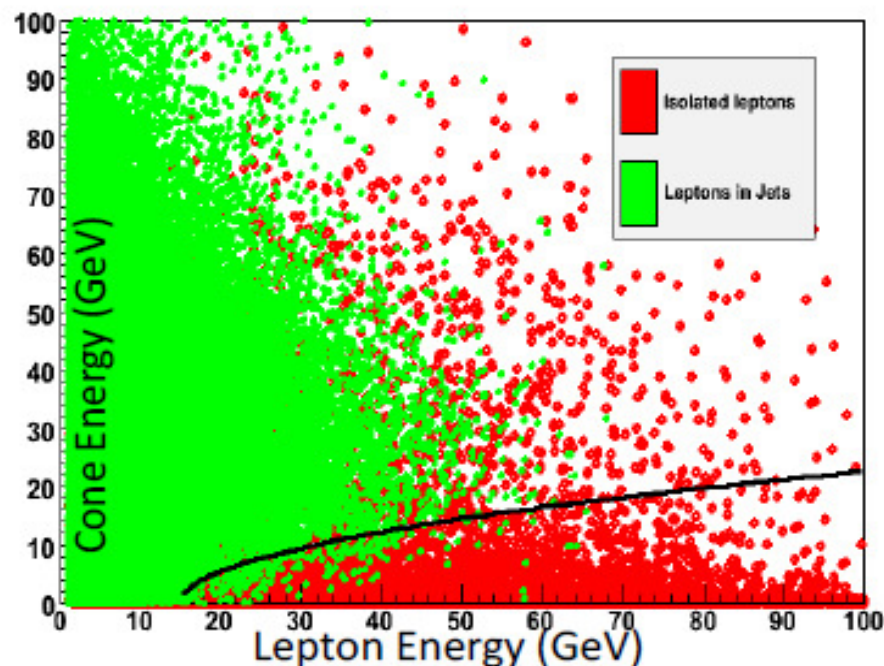


lepton selection / veto

- lepton identification by MC information (assuming high efficiency & purity for $E > 15$ GeV leptons)
- distinguish leptons inside a jet and those from top decay by summing the energy of the particles around the lepton
- 2-D selection (veto) of isolated leptons for the 6-jet + lepton analysis (8-jet analysis)



T. Tanabe



event shape

- use the thrust variable to discriminate signal from background

$$T = \max_{|\hat{n}|=1} \frac{\sum_i |\hat{n} \cdot \vec{p}_i|}{\sum_i |\vec{p}_i|}$$

jet clustering

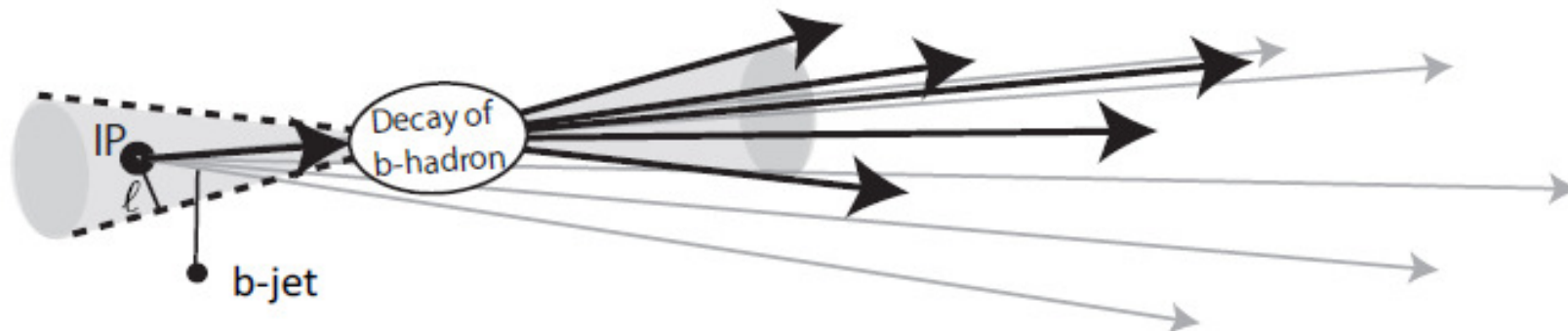
- we use the Durham jet clustering algorithm to force the event into the 6 (8) jet topology.

$$Y_{ij} = \frac{\max(E_i^2, E_j^2)(1 - \cos \theta_{ij})}{E_{\text{CM}}^2}$$

b-tagging

- identify b-jets via their large **impact parameter significance** (IPS) of secondary tracks.
- b-tagging criteria:
 - **tight (6J+L)**: require 4 tracks with IPS > 2.5
 - **tight (8J)**: require 2 tracks with IPS > 3.0
 - efficiency: 47%, fake rate: c-jet 3.2%, uds-jet 0.1%
 - **loose**: require 2 tracks with IPS > 2.0
 - efficiency: 80%, fake rate: c-jet 40%, uds-jet 0.5%
- event selection:
 - require at least 4 loose b
 - at least one tight b for Higgs candidate
 - one tight b for at least one top candidate

efficiency & fake rate
estimated on Z→qq
sample @ 91.2 GeV



jet combination

- choose the jet combination which is most consistent with the TTH mass hypothesis is chosen (minimize chi-squared):

$$\chi^2 = \frac{(m_{2j} - M_H)^2}{\sigma_H^2} + \frac{(m_{2j} - M_{W_1})^2}{\sigma_{W_1}^2} + \frac{(m_{3j} - M_{t_1})^2}{\sigma_{t_1}^2} + \left\{ \frac{(m_{2j} - M_{W_2})^2}{\sigma_{W_2}^2} + \frac{(m_{3j} - M_{t_2})^2}{\sigma_{t_2}^2} \right\}_{8j}$$